#### Detecting the boundaries of gravity anomaly sources using the vertical and tilt derivative

Snežana Ignjatović, Ivana Vasiljević, Branislav Sretković



#### Дигитални репозиторијум Рударско-геолошког факултета Универзитета у Београду

[ДР РГФ]

Detecting the boundaries of gravity anomaly sources using the vertical and tilt derivative | Snežana Ignjatović, Ivana Vasiljević, Branislav Sretković | The 55th International October Conference on Mining and Metallurgy , Kladovo, Serbia, 15 - 17. October 2024 | 2024 | |

DOI: 10.5937/IOC24099I

http://dr.rgf.bg.ac.rs/s/repo/item/0009287

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55<sup>th</sup> International October Conference on Mining and Metallurgy

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MINING AND METALLURGY INSTITUTE BOR and

# 55<sup>th</sup> International October Conference on Mining and Metallurgy

# PROCEEDINGS

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Ana Kostov

### 15 – 17 October 2024

Hotel "Đerdap" Kladovo, Serbia

## 55<sup>th</sup> International October Conference on Mining and Metallurgy

Editor:	Ana Kostov

Publisher: Mining and Metallurgy Institute Bor, 2024

**Printed in:** "GRAFOMED-TRADE" Bor

#### **Text printing**

preparation: Vesna Simić

**Disclaimer:** All full papers and abstracts submitted to the 55<sup>th</sup> International October Conference on Mining and Metallurgy (55 IOC) are subject to a peer reviewing process, using subject specialists selected because of their expert knowledge in the specific areas. Authors are responsible for the content, translation and

accuracy.

### **Circulation:** 150 copies

CIP – Каталогизација у публикацији Народна библиотека Србије, Београд

622(082) 669(082)

# INTERNATIONAL October Conference on Mining and Metallurgy (55; 2024; Kladovo)

Proceedings / 55th International October Conference on Mining and Metallurgy – IOC 2024, 15 – 17 October 2024, Kladovo, Serbia ; [organizers] Mining and Metallurgy Institute Bor [and] University of Belgrade, Technical Faculty in Bor ; editor Ana Kostov. - Bor : Mining and Metallurgy Institute, 2024 (Bor : Grafomed-trade). - XXI, 468 str. : ilustr. ; 24 cm

Tiraž 150. - Bibliografija uz svaki rad. - Registar.

ISBN 978-86-7827-053-6 а) Рударство -- Зборници b) Металургија -- Зборници

COBISS.SR-ID 153297161

#### Kladovo, 15 – 17 October 2024

Conference is financially supported by the Ministry of Science, Technological Development and Innovation of the Republic of Serbia, *Contract No. 451-03-4405/2024-03 from 08.07.2024.* 



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15 - 17 October 2024, Kladovo, Serbia https://ioc.irmbor.co.rs

DOI: 10.5937/IOC24099I

Original Scientific Paper-Geology

## DETECTING THE BOUNDARIES OF GRAVITY ANOMALY SOURCES USING THE VERTICAL AND TILT DERIVATIVE

#### Snežana Ignjatović<sup>1a</sup>, Ivana Vasiljević<sup>1b</sup>, Branislav Sretković<sup>1c</sup>

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#### Abstract

In geophysical exploration, it is important to define the boundaries of anomaly sources that are not visible on the surface. Information about the boundaries of sources can help during geophysicalgeological modeling of the survey area. A model of the survey area can help in better defining the geological structure and geological development of an exploration area. This paper presents how the procedures of vertical and tilt derivative on gravity data can help to detect the boundaries of anomaly sources. The Žagubica basin is taken as a study area. The results obtained for the survey area bring the new information.

Keywords: gravity data, boundary, Žagubica basin

#### **1. INTRODUCTION**

During geophysical–geological modeling of the survey area, it is particularly important to define the boundaries of anomaly sources under the surface. The results of the models can help in different explorations such as geology, archeology, exploration of the environment, civil engineering, etc.

This paper presents the procedure of vertical and tilt derivative to detect the boundaries of gravity anomaly sources. The Žagubica basin is used as a practical example.

The data for research were acquired from the Gravity Database of Serbia [1]. The geophysical software packages Oasis Montaj and Golden Software Surfer were used in processing and analysis the gravity data.

#### 2. THEORETICAL BACKGROUND AND FIELD EXAMPLE

The procedure of vertical derivative (first vertical derivative) and tilt derivative can help in detecting the boundaries of gravity anomalies sources.

The first vertical derivative (VDR) can be expressed as [2]:

 $VDR = -\partial f/\partial z$ ,

(1)

where f – gravity field (in paper the Bouguer anomaly),

 $\partial f/\partial z$  is the first-order derivative of the gravity field in the vertical direction z.

It is characteristic for the vertical derivative that it has zero over the boundaries, it is positive over the source and negative outside of a vertical side of the source [2, 3,4].



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The tilt derivative (TDR) is based on the ratio of the first vertical and total horizontal derivative [2, 3,4]

$$TDR = \tan^{-1} \left[ \frac{\frac{\partial g}{\partial z}}{\frac{\partial g}{\partial h}} \right], \tag{2}$$

where:

 $\partial^{g}/\partial h = \sqrt{(\partial g/\partial x)^{2} + (\partial g/\partial y)^{2}},$ 

 $\partial g/\partial x$ ,  $\partial g/\partial y$ ,  $\partial g/\partial z$  are the derivatives of the gravity g in the x, y, and z directions.

The TDR passes through zero above or near the boundaries, and it is positive when lying over the source structure and negative outside the source region [2, 3,4].

The Žagubica basin is used for a field example. The Žagubica basin is situated in east Serbia. The basin is located south of the Kučaj, Crni Vrh and Beljanica mountains, and north of the Homolje mountains. The Žagubica basin is composed of the Lower Cretaceous sediments and Upper Cretaceous sediments. In the survey area, the dominant structures have directions the NW-SE and NE-SW. These structures have a regional character and surround the basin. These structures influenced the formation and development of the Žagubica basin [5].



#### **3 RESULTS AND DISCUSSION**

Gravity data for the study area were obtained from the Gravity Database of Serbia [1]. The gravity data was used to create the Bouguer anomaly (gravity anomaly) map. The Bouguer anomaly map was done with a density value of 2.40 t/m<sup>3</sup>. The data filtering was done to eliminate or reduce errors and disturbances in the measured signal. The filtered map of the Bouguer anomaly is shown in Figure 2. This map is the basis for further processing data.

The minimum values of anomalies were detected in the east and central parts of the map (Figure 2). A source of anomaly in the central part is the Žagubica basin (Figure 1).



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The source of anomaly in the east part is the part of the Žagubica basin which is not detected on the surface. These minimum values of anomalies indicate existence of two basins under the surface.





Figure 2. Filtered map of the Bouguer anomaly

For detecting the boundaries of these gravity anomaly sources, the procedures of vertical and tilt derivative are applied. The procedure VDR and TDR are applied on the Bouguer anomaly map.

The results of the vertical derivative are shown in Figure 3. In the east and central parts of the map, the black dash lines mark the positions of boundaries of anomaly sources. The results of VDR show existence of two basins under the surface.



Figure 3. Map of vertical derivative (black dash lines – boundaries of anomaly sources)

Figure 4 shows the results of tilt derivative. The positions of the boundaries of anomaly sources are marked with the red dash lines in the east and central parts of the map. The results of TDR indicated that under the surface exist two basins.



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**Figure 4.** *Map of tilt derivative (red dash lines – boundaries of anomaly sources)* 

#### 4. CONCLUSION

The positions of the boundaries of anomaly sources can be detected and defined using the procedures VDR and TDR on gravity data. The results in this paper bring the new information about the Žagubica basin. The results of VDR and TDR show the existence of two separate basins in the subsurface. These results can help to better defining the geological development of a survey area.

#### ACKNOWLEDGEMENTS

The authors would like to thank the Ministry of Science, Technological Development and Innovation for providing resources under Contract No. 451-03-65/2024-03/200126.

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